



USING CONSTRAINT  
PROGRAMMING  
TO VERIFY UML / OCL MODELS  
*A SHORT SURVEY*

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# Summary

- Introduction
  - Constraint Satisfaction Problems (CSPs)
  - UML / OCL
- Principles for using CSP to check UML / OCL models.
- Turning UML class diagrams into CSP (1)
- Turning UML class diagrams into CSP (2)
- Conclusion & references

# Constraint Satisfaction Problem (1 / 2)

- A CSP is expressed as :
  - Variables  $v_i$
  - Finite domains  $D_i = \{ d_1, d_2, \dots, d_{k(i)} \}$
  - Relations, which always hold, among variables:  $C_j$
  - (Cost  $f$ )
- Example : SEND + MORE = MONEY
- Goal: For each  $v_i$ , find one value  $d_k$  from  $D_i$  which together satisfy every  $C_j$ . (And which minimizes  $f$ .)

# Constraint Satisfaction Problem (2 / 2)

- Algorithm FIND-FIRST:
  1. Choose an unassigned variable  $v_i$
  2. Choose a value  $d_k$  from  $v_i$ 's domain  $D_i$
  3.  $v_i \leftarrow d_k$
  4. Propagate through  $C_j$  [NP complete]
    - IF there exists an empty domain  $D_l$ , THEN
      - a. UNDO propagation of step 4
      - b. UNDO assignment of step 3
      - c. IF all assignments  $(v_i, d_k)$  have already been tried THEN FAILURE
      - d. GOTO step 2 or step 1
  5. IF there exists a variable  $v_j$  which is not assigned THEN GOTO 1.
  6. SUCCESS
- Backtrack after step 6 : algorithm ENUMERATE.
  - Cost  $f$ : Constraint Satisfaction and Optimization Problem (CSOP).
- Packages: CHOCO from Bouygues' e-lab, (J)SOLVER from IBM (ex-ILOG), ECLIPSE from IC PARC, CHIP from COSYTEC, AQL from INOVIA, PROLOG IV from univ. Marseille, SICSTUS PROLOG, etc.

# Unified Modeling Language (UML)

- Graphical modeling language in object-oriented software engineering.
- Standard of the OMG since 1997.
- Diagrams :
  - Structural (7): Class diagram, ...
  - Behavioral (3): Use case diagram, ...
  - Interaction (4): Sequence diagram, ...
- Meta-modeling architecture: Meta-Object Facility.



# Object Constraint Language

- Object-oriented.
- Specified by the OMG
- Used on UML diagrams
- Can represent:
  - Invariants:
    - Predicate which must always hold.
  - Pre- (resp. post-) conditions:
    - Predicate which must hold before (resp. after) an operation.
  - Result of a method (body):
    - The type of a context's result = type of the result of the designated operation.
  - Initial / derived value of an attribute.
  - ...

# Uses of CSP for checking UML / OCL models

- Uses:
  - Checking that a model (either hand written or generated ) verifies the constraints of a meta-model.
    - Dresden OCL Toolkit (univ. Dresden).
  - Generating a sequence of tests
    - A model includes constraints on specifications or tests of an application.
    - Smart Testing.
- Avoiding bugs in class diagrams !
  - Bug: Zero possible instances of a class !
  - Bug: Mismatch in multiplicity of associations !

# Turning class diagrams into CSP

- **Satisfiability:**
  - Definition: A user can possibly create a set of new objects and links over the classes and associations of the model, so that no model constraint is violated.
- A CSP has a solution  $\Leftrightarrow$  the model is satisfiable.
- **Variants:**
  - Strong satisfiability: The model must have a finite instantiation where the population of each class and association is at least one.
  - Weak satisfiability: same as above, but for « at least one class ».
  - Liveliness of a class c: same as above, but « where the population in c is non empty ».



# Turning class diagrams into CSP

## The CSP model: Classes

- CSP variables:
  - A list variable *InstanceC* :
    - $struct(c) = (oid, f_1, \dots, f_n)$
  - An integer variable *SizeC* (arbitrarily upper bounded).
- CSP constraints:
  - Number of links:  $SizeC = length(InstanceC)$
  - Uniqueness of identifiers:  $cx \neq cy \Rightarrow cx.oid \neq cy.oid$

# Turning class diagrams into CSP

## The CSP model: Associations

- Variables:
  - A list variable *InstanceAS*:
    - $struct(InstanceAS) = (p_1, \dots, p_n)$  where  $p_i$  = role of class
  - A integer variable *SizeAS* (arbitrarily upper-bounded)
- Constraints:
  - Number of links:  $SizeAS = length(InstanceAS)$
  - Existence of referenced objects:  $link.p_i = x.oid$

# Turning class diagrams into CSP

## The CSP model: Associations (cont'd)



- CSP constraints (followed):
  - Cardinalities:
    - $SizeAS < SizeClassX * SizeClassY$
    - $minClassXAS * SizeClassY < SizeAS < maxClassXAS * SizeClassY$
    - $minClassYAS * SizeClassX < SizeAS < maxClassYAS * SizeClassX$
  - Multiplicities of associations:
    - $minClassXAS < \#\{instanceAS.p1 = instanceClassX\} < maxClassXAS$
    - $minClassYAS < \#\{instanceAS.p2 = instanceClassY\} < maxClassYAS$

# Turning class diagrams into CSP (4/6)

## The CSP model: the ISA hierarchy

- No new CSP variables.
- CSP constraints:
  - Existence of instances in supertype:
    - $InstanceSub.oid = InstanceSup.oid$
  - Number of instances:  $SizeClassSub < SizeClassSup$
  - Disjointness for a sup  $Csup$  and subs  $Csub_i$ 
    - $SizeCsup > sum( SizeCsub_i )$
    - $ObjectI.oid = ObjectJ.oid \Rightarrow I = J$
  - Completeness of a super
    - $SizeCsup < sum( SizeCsub_i )$
    - $ObjectSup.oid = ObjectSub.oid$

# Turning class diagrams into CSP (5/6)

## The CSP model: OCL constraints

- Invariants.
- Expressed in ECLIPSE Prolog.
  - Less direct!
- An OCL constraint is considered as an instance of the OCL meta-model
  - A node corresponds to constants and variables of the constraint.

# Turning class diagrams into CSP (6/6)

## Implementation

- (1) Finding the sizes ; then (2) finding the instances.
- ECLIPSE and JAVA libraries, extending Dresden OCL.
- Tool UMLtoCSP <http://gres.uoc.edu/UMLtoCSP/>

# A second way to solve the same problem

- Principle : represent class diagrams in Description Logics (concepts, roles, individuals) and use a CSP engine as a reasoner.
  - Finite satisfiability problem.
  - Binary associations.
  - No OCL constraints.
- Sketch of the CSP model:
  - A variable is the number of instances of a class.
  - Another variable is the number of associations.
  - Constraints are inequalities among variables.
  - ISA hierarchies with associations lead to an explosion of variables.
- Experiments with OPL Studio (SOLVER) on Common Information Models (management information on a network/company).

# Conclusion

- Goal: Avoiding bugs in UML / OCL models
  - A class with zero possible instances.
  - Mismatch in multiplicity of associations.
- Turning a class diagram into a CSP.
  - An UML / OCL model is satisfiable  $\Leftrightarrow$  a CSP has a solution.
  - Automatically generating a CSP: Representing classes, associations, ISA hierarchy as variables and constraints.
  - Solving the CSP with an off-the-shelf constraint engine.
- Future work:
  - Other UML diagrams ?
  - Other OCL constraints ?
  - Scaling up ? (e.g., n x 100 classes)
  - Using a SAT-solver. What about MIP, evolutionnary algorithms, ... ?



# References

1. Cabot, J.; Clariso, R.; Riera, D.; Verification of UML/OCL Class Diagrams using Constraint Programming. [Software Testing Verification and Validation Workshop, 2008. ICSTW '08. IEEE International Conference, 2008.](#)
2. Marco Cadoli, Diego Calvanese, Giuseppe De Giacomo, Toni Mancini. Finite Model Reasoning on UML Class Diagrams Via Constraint Programming. [AI\\*IA 2007: Artificial Intelligence and Human-Oriented Computing Lecture Notes in Computer Science](#), 2007, Volume 4733/2007, 36-47.
3. Mathias Soeken, Robert Wille, Mirco Kuhlmann, Martin Gogolla, Rolf Drechsler, Verifying UML/OCL models using Boolean satisfiability. Proceedings of the Conference on Design, Automation and Test in Europe, 2010.

THANK YOU FOR YOUR  
ATTENTION !

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